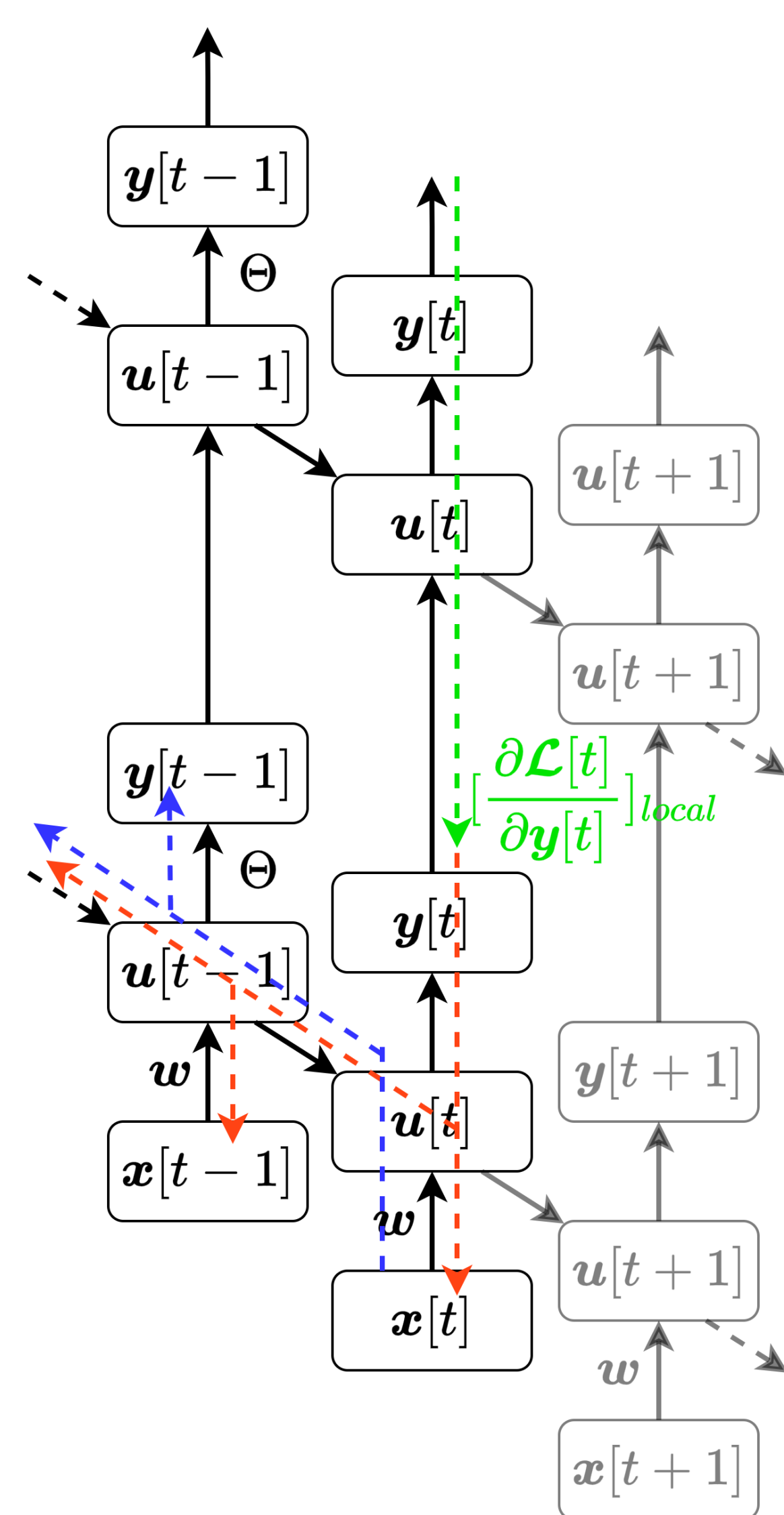




## Motivation

- Backpropagation-through-time (BPTT) assigns temporal credit but scales with timesteps  $T$ , inflating memory and compute in SNNs. We want a **temporal-local** rule that preserves rich spike-timing cues while avoiding BPTT's unfolding.

## Method Overview



$$\Delta w[t] = \left[ \frac{\partial \mathcal{L}}{\partial y[t]} \right] \alpha_{pre} \Psi(u[t]) \sum_{t'=0}^t \lambda_{pre}^{t-t'} x[t'] + \alpha_{post} x[t] \sum_{t'=0}^{t-1} \lambda_{post}^{t-t'} \Psi(u[t'])$$

**S-TLLR** is a three-factor update: an instantaneous eligibility trace that blends **causal** (pre $\rightarrow$ post) and **non-causal** (post $\rightarrow$ pre) terms, modulated by a **global learning signal**  $\delta[t]$  (via BP-through-layers or DFA). No time-unrolling or state per-synapse is kept.

## Key Ideas

- **Temporal locality:** forward-only computation; time-constant memory  $O(n)$ .
- **Balanced timing:**  $\alpha_{pre}$  (causal) +  $\alpha_{post}$  (non-causal) improves generalization.
- **Flexible  $\delta$ :** BP/DFA at layer level; late  $\delta$  reduces MACs with minor accuracy impact.

## Experiments

S-TLLR matches or surpasses BPTT on event-vision and audio benchmarks while using *far less* memory; late  $\delta$  further reduces compute.

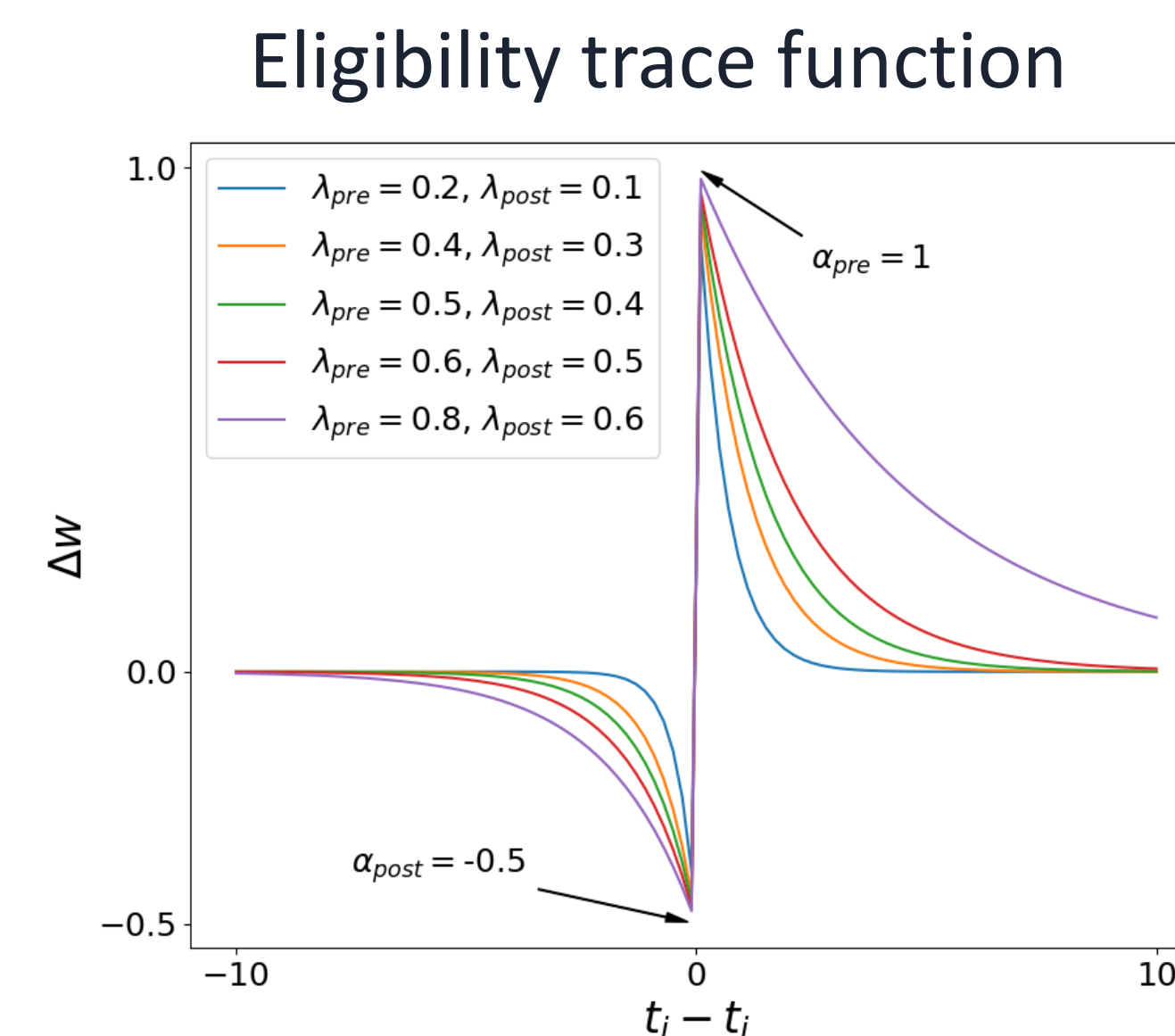


Table 1. Effects of including the non-causal terms in the eligibility traces

Dataset	Model	T	T <sub>l</sub>	$\alpha_{post} = 0$	$\alpha_{post} = +1$	$\alpha_{post} = -1$
DVS Gesture	VGG9	20	15	94.61 $\pm$ 0.73%	94.01 $\pm$ 1.10%	<b>95.07 <math>\pm</math> 0.48%</b>
DVS CIFAR10	VGG9	10	5	72.93 $\pm$ 0.94%	73.42 $\pm$ 0.50%	<b>73.93 <math>\pm</math> 0.62%</b>
N-CALTECH101	VGG9	10	5	62.24 $\pm$ 1.22%	53.42 $\pm$ 1.50%	<b>66.33 <math>\pm</math> 0.86%</b>
SHD	RSNN	100	10	77.09 $\pm$ 0.33%	<b>78.23 <math>\pm</math> 1.84%</b>	74.69 $\pm$ 0.47%

Table 2. Accuracy performance of methods on vision and audio datasets

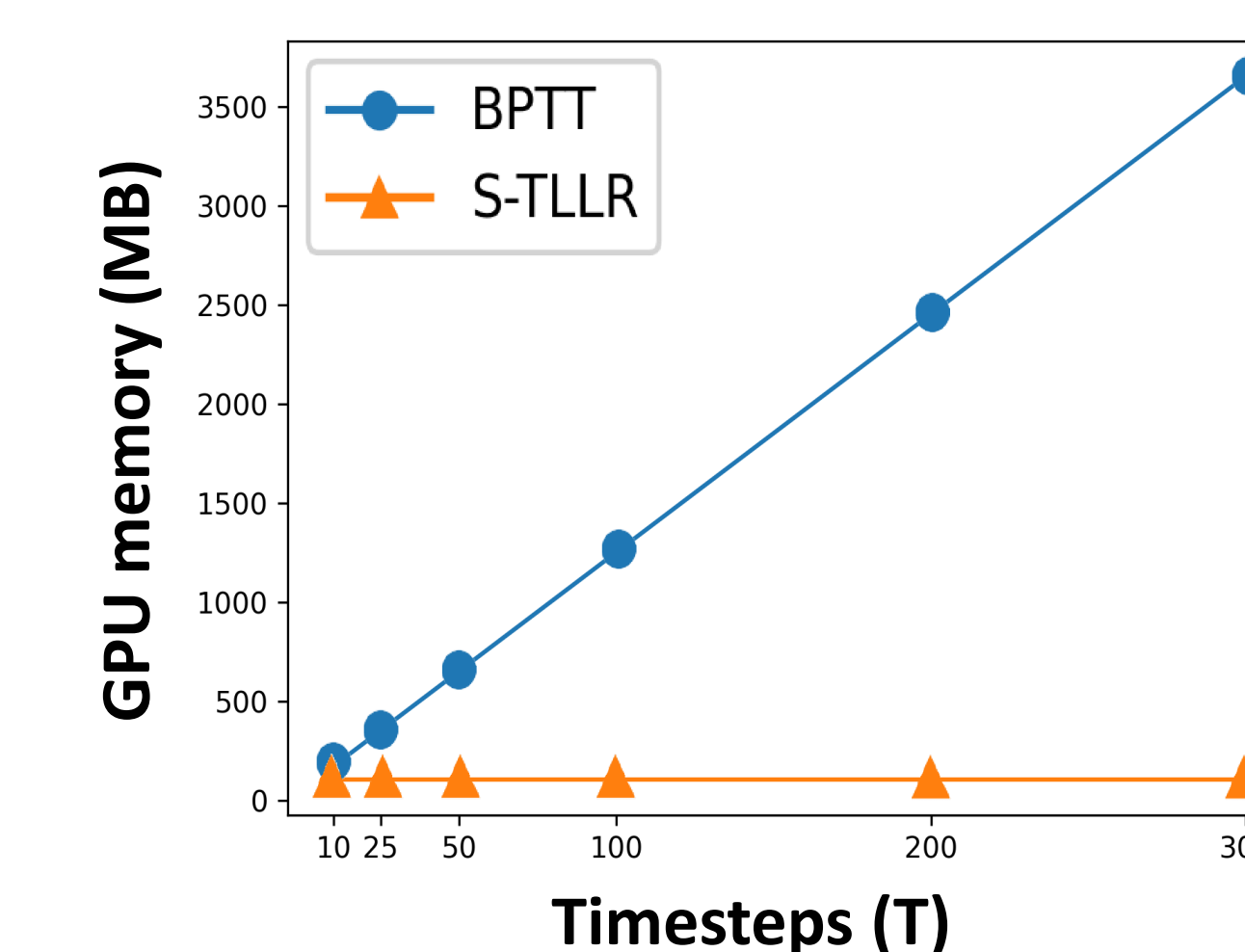
Method	Model	Accuracy (mean $\pm$ std)	# MAC <sup>1</sup> ( $\times 10^9$ )	Memory <sup>1</sup> (MB)
DVS CIFAR10				
TET (Deng et al., 2022)	VGG-11	83.17 $\pm$ 0.15%	-	-
DSR (Meng et al., 2022)	VGG-11	77.27 $\pm$ 0.24%	-	-
BPTT (Li et al., 2021)	ResNet-18	75.4 $\pm$ 0.05%	-	-
OTTT <sub>A</sub> (Xiao et al., 2022)	VGG-9	76.27 $\pm$ 0.05%	-	-
BPTT (baseline)	VGG-9	75.44 $\pm$ 0.76%	6.82	18.12
S-TLLR (Ours, T <sub>l</sub> = 5, $\alpha_{post} = -1$ )	VGG-9	73.93 $\pm$ 0.62%	5.12	3.62
S-TLLR (Ours, T <sub>l</sub> = 0, $\alpha_{post} = -1$ )	VGG-9	75.6 $\pm$ 0.10%	10.26	3.62
S-TLLR (Ours, T <sub>l</sub> = 0, $\alpha_{post} = 0$ )	VGG-9	74.8 $\pm$ 0.15%	6.82	3.62
BPTT (baseline)	ResNet18	72.68 $\pm$ 0.87%	7.13	28.14
S-TLLR (Ours, T <sub>l</sub> = 5)	ResNet18	71.94 $\pm$ 0.75%	5.12	5.62
S-TLLR (Ours, T <sub>l</sub> = 0)	ResNet18	74.5 $\pm$ 0.64%	10.24	5.62
DVS Gesture				
SLAYER (Shrestha & Orchard, 2018)	SNN (8 layers)	93.64 $\pm$ 0.49%	-	-
DECOLLE (Kaiser et al., 2020)	SNN (4 layers)	95.54 $\pm$ 0.16%	-	-
OTTT <sub>A</sub> (Xiao et al., 2022)	VGG-9	96.88%	-	-
BPTT (baseline)	VGG-9	95.58 $\pm$ 1.08%	6.06	16.13
S-TLLR (Ours)	VGG-9	97.72 $\pm$ 0.38%	2.27	1.61
BPTT (baseline)	ResNet18	94.92 $\pm$ 0.38%	6.34	25.03
S-TLLR (Ours)	ResNet18	94.92 $\pm$ 0.61%	2.27	2.50
N-CALTECH101				
BPTT (She et al., 2022)	SNN (12 layers)	71.2%	-	-
BPTT (Kim et al., 2023)	VGG-16	64.40%	-	-
BPTT (baseline)	VGG-9	65.92 $\pm$ 0.82%	22.81	20.15
S-TLLR (Ours)	VGG-9	66.058 $\pm$ 0.92%	17.22	4.03
BPTT (baseline)	ResNet18	60.89 $\pm$ 0.89%	6.34	31.31
S-TLLR (Ours)	ResNet18	61.65 $\pm$ 0.99%	4.27	6.26
SHD				
ETLP (Quintana et al., 2023)	ALIF-RSNN	74.59 $\pm$ 0.44%	-	-
OSTTP (Ortner et al., 2023)	LIF-RSNN	77.33 $\pm$ 0.8%	-	-
BPTT (Bouanane et al., 2022)	LIF-RSNN	83.41	-	-
BPTT (Cramer et al., 2022)	LIF-RSNN	83.2 $\pm$ 1.3	-	-
BPTT (baseline)	LIF-RSNN	70.57 $\pm$ 0.96	0.054	0.961
S-TLLR <sub>BP</sub> (Ours)	LIF-RSNN	78.24 $\pm$ 1.84%	0.096	0.019
S-TLLR <sub>DFA</sub> (Ours)	LIF-RSNN	74.60 $\pm$ 0.52%	0.096	0.019

## Advantages Over Existing Techniques

- **Time-local updates:** no gradient backprop through time.
- **Lower Memory:**  $O(n)$  vs  $O(T \cdot n)$  activations for BPTT.
- **Task-adaptive timing:** tune  $\alpha_{post}$  sign for spatial vs temporal tasks.

Table 3. Comparison with learning methods

Method	Memory Complexity	Time Complexity	Temporal Local	Leverage Non-Causality
BPTT	$Tn$	$Tn^2$	$\times$	$\times$
RTRL	$n^3$	$n^4$	$\checkmark$	$\times$
e-prop	$n^2$	$n^2$	$\checkmark$	$\times$
OSTL	$n^2$	$n^2$	$\checkmark$	$\times$
ETLP	$n^2$	$n^2$	$\checkmark$	$\times$
OSTTP	$n^2$	$n^2$	$\checkmark$	$\times$
OTTT	$n$	$n^2$	$\checkmark$	$\times$
S-TLLR	$n$	$n^2$	$\checkmark$	$\checkmark$



**Temporal-local rule**  
→ **constant memory footprint**, enabling long-sequence training on resource-limited hardware.

## Takeaways

- Competitive accuracy with markedly reduced memory (up to  $10 \times$ ).
- Late learning signal yields  $1.3 - 6.6 \times$  fewer MACs.
- Simple to implement; works for feedforward, CNN, and recurrent SNNs.

## ACKNOWLEDGMENT

This work was supported in part by the Center for CoDesign of Cognitive Systems (CoCoSys), one of seven centers in JUMP 2.0, funded by the Semiconductor Research Corporation (SRC) and DARPA, in part by the MicroE4AI program of IARPA, the DoE Microelectronics program, the National Science Foundation, and Intel Corporation.